

P3

3. PRAKTIKA: KURBEN ADIERAZPENA FORMA INPLIZITUAN

▼ Proposatutako Ariketa P-3.1

Ondorengo kurba familia emanik:

$$1=5x^2+4y^2; 0=15-7x^2-5y^2$$

- Irudikatu funtzioak ardatz berdinak erabilia.
- Grafiko bakoitza kolore ezberdin bat erabilia marraztu.
- Funtzio bakoitzari etiketa ezberdin bat jarri.
- Irudiaren inguruko laukia kendu eta ardatzak jarri.

▼ Soluzioa P-3.1

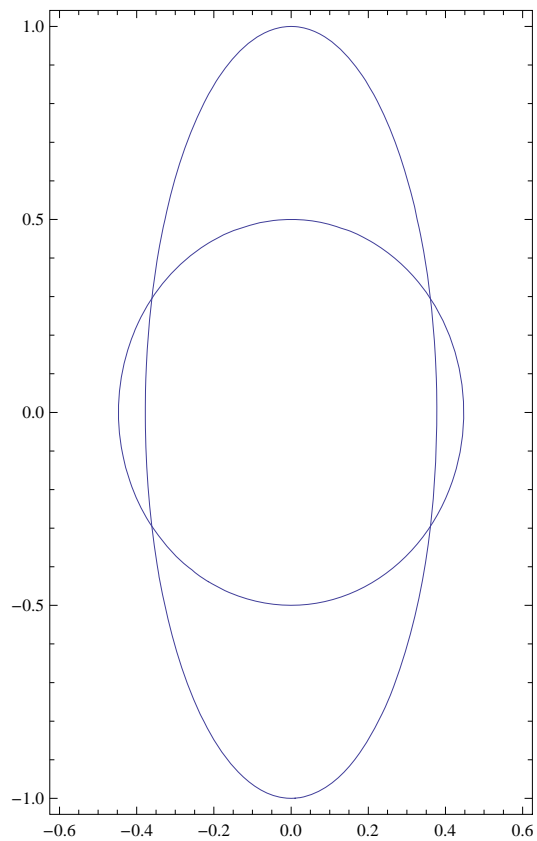
★ a) Funtzioak definituko ditugu eta ardatz berdinak erabilia adieraziko ditugu

$$f1[x_, y_] = 5 x^2 + 4 y^2 - 1; f2[x_, y_] = 1 - 7 x^2 - y^2;$$

$$g1 = \text{ContourPlot}[f1[x, y] == 0, \{x, -0.6, 0.6\}, \{y, -1, 1\}];$$

$$g2 = \text{ContourPlot}[f2[x, y] == 0, \{x, -0.6, 0.6\}, \{y, -1, 1\}];$$

```
Show[{g1, g2}, AspectRatio -> Automatic]
```



★ b) **Funtzio bakoitzari kolore ezberdin bat emango diogu**

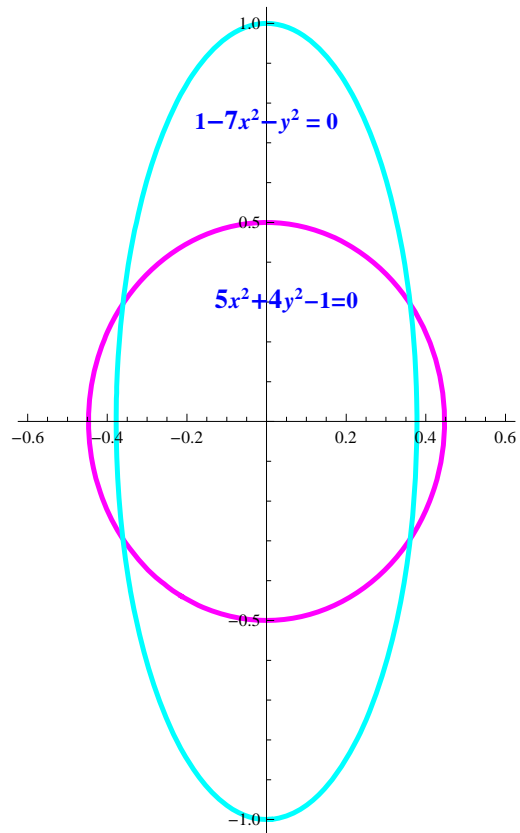
```
g1 = ContourPlot[f1[x, y] == 0, {x, -0.6, 0.6},
  {y, -1, 1}, ContourStyle -> {Thickness[0.01], Magenta}];
g2 = ContourPlot[f2[x, y] == 0, {x, -0.6, 0.6}, {y, -1, 1},
  ContourStyle -> {Thickness[0.01], Cyan}];
Show[{g1, g2}, AspectRatio -> Automatic];
```

★ c) **Etiketak jarriko ditugu**

```
Show[{g1, g2}, AspectRatio -> Automatic,
  Epilog -> {Text[Style["5x2+4y2-1=0", Medium, Bold, Blue], {0.05, 0.3}],
  Text[Style["1-7x2-y2 = 0", Medium, Bold, Blue], {0.0, .75}]}];
```

★ d) Inguruko laukia kendu eta ardatzak erantsiko ditugu

```
Show[{g1, g2}, AspectRatio -> Automatic, Axes -> True, Frame -> False,
  Epilog -> {Text[Style["5x2+4y2-1=0", Medium, Bold, Blue], {0.05, 0.3}],
  Text[Style["1-7x2-y2 = 0", Medium, Bold, Blue], {0.0, .75}]}]
```



▼ Proposatutako Ariketa P-3.2

- a) Definitu $f(x,y) = \sin(x)\sin(y) - 0,5$ eta $g(x,y) = \cos(x)\cos(y) - 0,5$ funtzioak.
- b) Egin $f(x,y)$ funtzioaren adierazpen grafikoa eta baita ere $f(x,y) = 0$ eta $g(x,y) = 0$ -rena ere, ardatz berdinek erabilia, bakoitzari kolore ezberdinak egokituta eta grafikoaren atzealdeari ere kolore bat egokituta.

▼ Soluzioa P-3.2

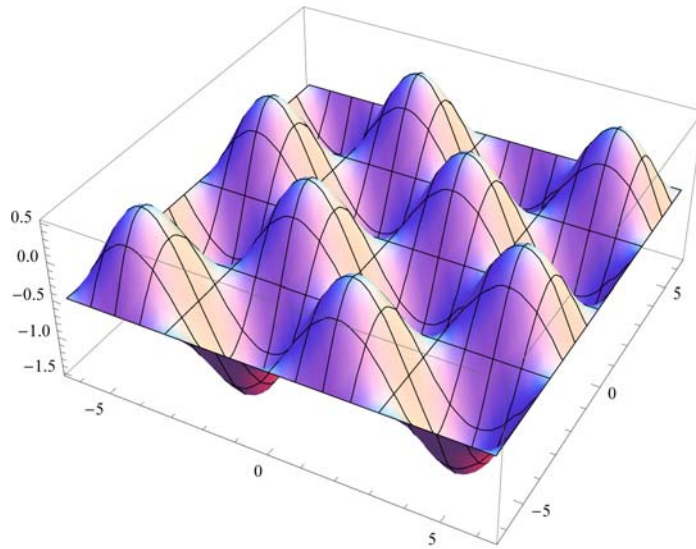
★ a) Funtzioen definizioa

$$f[x_, y_] = \text{Sin}[x] * \text{Sin}[y] - 0.5;$$

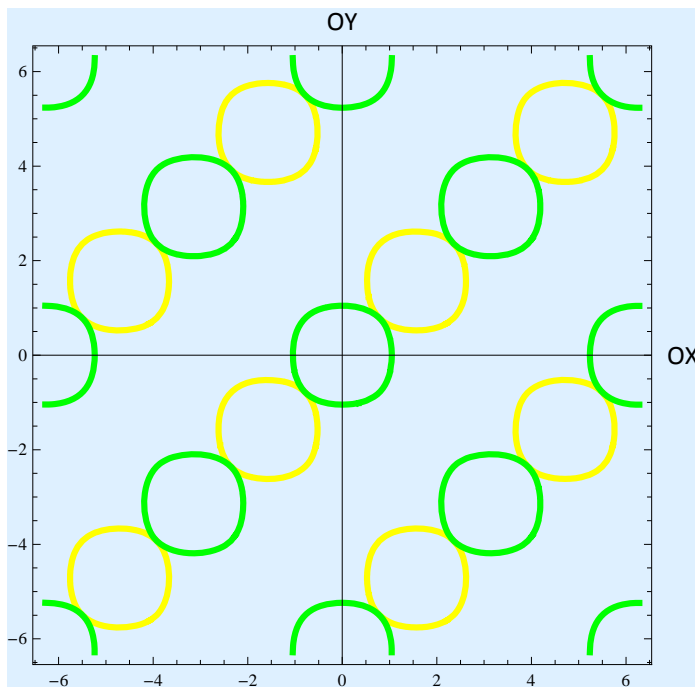
$$g[x_, y_] = \text{Cos}[x] * \text{Cos}[y] - 0.5;$$

★ b) $f(x,y)$ funtzioaren adierazpen grafikoa

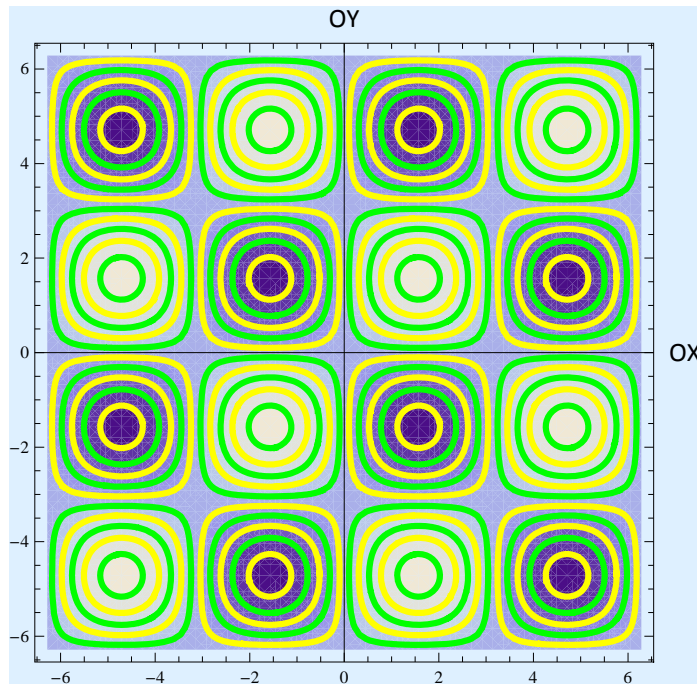
```
Plot3D[{f[x, y]}, {x, -2 π, 2 π}, {y, -2 π, 2 π}]
```

★ b) $f(x,y)=0$ eta $g(x,y)=0$ -ren adierazpen grafikoa

```
ContourPlot[{f[x, y] == 0, g[x, y] == 0}, {x, -2 π, 2 π}, {y, -2 π, 2 π},  
ContourStyle -> {{Thickness[0.01], Yellow}, {Thickness[0.01], Green}},  
Axes -> True, AxesLabel -> {"OX", "OY"}, Background -> LightBlue]
```

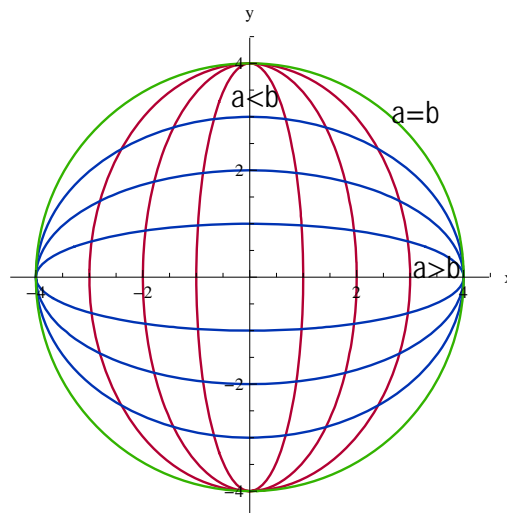


```
ContourPlot[{f[x, y]}, {x, -2 π, 2 π}, {y, -2 π, 2 π},
  ContourStyle → {{Thickness[0.01], Yellow}, {Thickness[0.01], Green}},
  Axes → True, AxesLabel → {"OX", "OY"}, Background → LightBlue]
```



▼ Proposatutako Ariketa P-3.3

Marraztu ondorengo elipse familia:



▼ Soluzioa P-3.3

```
a = ContourPlot[{y^2 / 16 + x^2 / 1 == 1, y^2 / 16 + x^2 / 4 == 1, y^2 / 16 + x^2 / 9 == 1},
  {x, -4, 4}, {y, -4, 4}, Frame → False, Axes → True, AxesLabel → {"x", "y"},
  ContourStyle → {{RGBColor[0.7, 0, 0.2], Thickness[0.005]},
  {RGBColor[0.7, 0, 0.2], Thickness[0.005]}, {RGBColor[0.7, 0, 0.2],
  Thickness[0.005]}, {RGBColor[0.7, 0, 0.2], Thickness[0.005]}}];
```

```

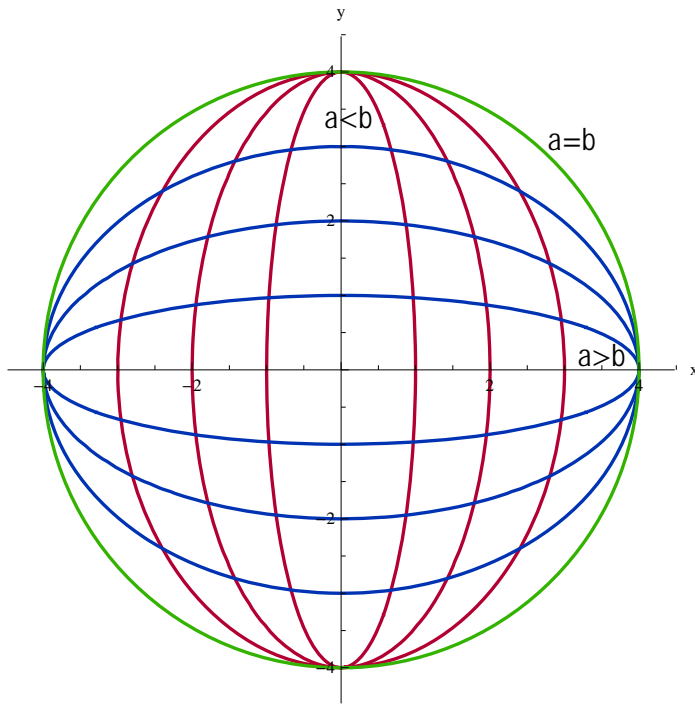
b = ContourPlot[{x^2/16 + y^2/1 = 1, x^2/16 + y^2/4 = 1, x^2/16 + y^2/9 = 1},
  {x, -4, 4}, {y, -4, 4}, Frame -> False, Axes -> True, AxesLabel -> {"x", "y"},
  ContourStyle -> {{RGBColor[0, 0.2, 0.7], Thickness[0.005]}, {RGBColor[0, 0.2, 0.7],
  Thickness[0.005]}, {RGBColor[0, 0.2, 0.7], Thickness[0.005]}}];

c = ContourPlot[{x^2 + y^2 = 16}, {x, -4, 4}, {y, -4, 4}, Frame -> False, Axes -> True,
  AxesLabel -> {"x", "y"}, ContourStyle -> {{RGBColor[0.2, 0.7, 0], Thickness[0.005]}}];

etiketak = {Text["a=b", {3.1, 3.1}], Text["a>b", {3.5, 0.2}], Text["a<b", {0.1, 3.4}]}];

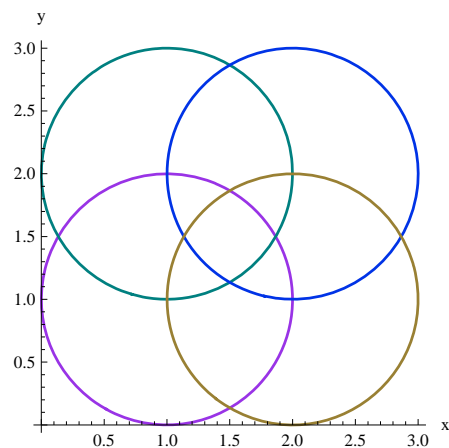
Show[a, b, c, PlotRange -> {{-4.3, 4.3}, {-4.3, 4.3}}, Epilog -> Graphics[etiketak][[1]]

```



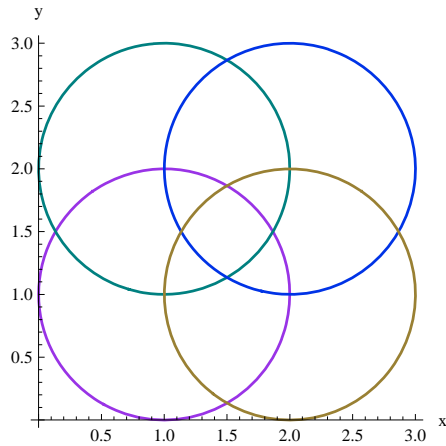
▼ Proposatutako Ariketa P-3.4

Irudikatu ondorengo zirkunferentzia familia:



▼ Soluzioa P-3.4

```
a = ContourPlot[
  {(x - 1)^2 + (y - 1)^2 == 1, (x - 1)^2 + (y - 2)^2 == 1, (x - 2)^2 + (y - 2)^2 == 1, (x - 2)^2 + (y - 1)^2 == 1},
  {x, 0, 3}, {y, 0, 3}, ContourStyle -> {{RGBColor[0.6, 0.2, 0.9], Thickness[0.007]},
    {RGBColor[0, 0.5, 0.5], Thickness[0.007]}, {RGBColor[0, 0.2, 0.9],
    Thickness[0.007]}, {RGBColor[0.6, 0.5, 0.2], Thickness[0.007]}},
  Axes -> True, AxesLabel -> {"x", "y"}, Frame -> False]
```



▼ Proposatutako Ariketa P-3.5

Ardatz berdinak erabilia irudikatu:

$$x^2 + y^2 = 1; x^2 + y^2 = 4 \text{ eta } x^2 + y^2 = 9$$

bakoitza kolore ezberdin bat erabilia. Grafikoari "zirkunferentziak" izena jarri, inguruko laukia kendu, ardatzak gehitu eta izenak jarri.

▼ Solución P-3.5

```
a = ContourPlot[{x^2 + y^2 == 1, x^2 + y^2 == 4, x^2 + y^2 == 9},  
  {x, -3, 3}, {y, -3, 3}, ContourStyle →  
  {{Thickness[0.01], Blue}, {Thickness[0.01], Green}, {Thickness[0.01], Orange}},  
  Axes → True, Frame → False, AxesLabel → {"OX", "OY"}, PlotLabel → Style[  
  Framed["ZIRKUNFERENTZIAK"], 16, Blue, Background → Lighter[LightYellow]]]
```

