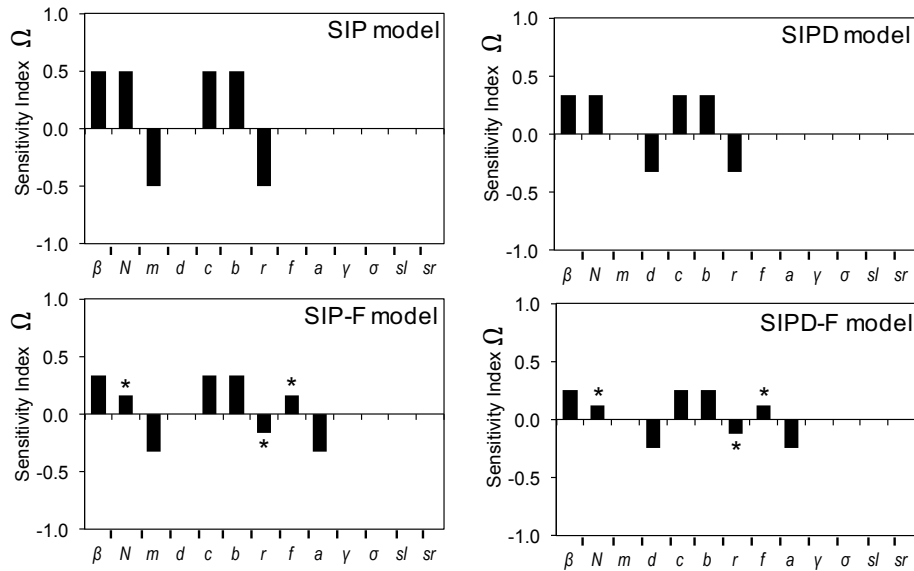


## Solution to Exercise 5. Sensitivity analysis of $R_0$ for SIP, SIPD, SIPF and SIPDF models

As in Lesson 6, local sensitivity of  $R_0$  for each model has been analyzed through the sensitivity index  $\Omega$ . The normalized sensitivity index of  $R_0$  with respect to any parameter  $p_i$  at a fixed value  $p^0$  is

$$\Omega_{p_i}^{R_0} = \frac{\partial R_0}{\partial p_i} \times \frac{p_i}{R_0} \Big|_{p_i=p^0} \quad (1)$$

The parameter values have been selected uniformly distributed (i.e. at increments of 10%) over the parameter's full or at least wide range of feasible values. The sensitivity index of  $R_0$  models for each parameter is presented in Figure 1 as the solution to Exercise 5.



**Figure 1:** Sensitivity analysis (SA) of  $R_0$  to the parameters for the models SIP, SIPD, SIPF and SIPDF. The sensitivity index represents the unit  $R_0$  change per unit change in the given parameter. The asterisks mark parameters for which the sensitivity index was not constant over the evaluated range. For these parameters, the sensitivity index obtained for the baseline value of the parameter is shown.

The analysis for each parameter was computed at a 0-1 parameter range for all parameters except for  $b$  (0-10000), and  $N$  (0-200), while the rest of the parameters were held constant with these baseline values:  $\beta = 0.001$ ,  $m = 0.1$ ,  $d = 0.1$ ,  $c = 0.1$ ,  $b = 10000$   $r = 0.1$ ,  $a = 0.1$ ,  $f = 0.001$ ,  $N = 100$ .