



### Problem 5.-

Settling velocity for different diameters:

-  $d = 2 \text{ mm}$

$$v_s = \frac{9.8 \frac{\text{m}}{\text{s}^2} \cdot \left( 2650 \frac{\text{kg}}{\text{m}^3} - 1000 \frac{\text{kg}}{\text{m}^3} \right) \cdot (2 \cdot 10^{-3} \text{m})^2}{18 \cdot 9.95 \cdot 10^{-4} \text{ Pa} \cdot \text{s}} = 3.6114 \frac{\text{m}}{\text{s}}$$

-  $d = 1 \text{ mm}$

$$v_s = 0.9029 \frac{\text{m}}{\text{s}}$$

-  $d = 0.5 \text{ mm}$

$$v_s = 0.2257 \frac{\text{m}}{\text{s}}$$

-  $d = 0.3 \text{ mm}$

$$v_s = 0.0812 \frac{\text{m}}{\text{s}}$$

-  $d = 0.2 \text{ mm}$

$$v_s = 0.0361 \frac{\text{m}}{\text{s}}$$

Settling time:

$$t_s = \frac{H}{V_s} = \frac{2.1 \text{ m}}{V_s(\text{particles})}$$

Length needed for total settling:

$$L_{100} = t_s \cdot v_0$$

$$v_0 = \frac{Q}{\text{Section}} = \frac{1.05902 \frac{\text{m}^3}{\text{s}}}{1.5 \text{ m} \cdot 2.1 \text{ m}} = 0.336 \frac{\text{m}}{\text{s}}$$

d (mm)	$t_s$ (s)	$L_{100}$ (m)	$\eta = \frac{L_{\text{real}}}{L_{100}} \cdot 100$	$\eta_i \cdot m_i$
2	0.5815	0.1955	4654% (>100%)	40
1	2.3260	0.7820	1163% (>100%)	25
0.5	9.3039	3.1280	290% (>100%)	20
0.3	25.8442	8.6888	104% (>100%)	10
0.2	58.1494	19.5498	46%	2.327 (5x0.46)



$\sum \eta_i \cdot m_i = 97.33\% \rightarrow$  Yes, it is adequate to remove at least 80% of the sand.

### Problem 6.-

a) Diameter and depth of settling tank

$$S = \pi r^2 ; S = \frac{Q}{F_c}$$

$$\pi \frac{d^2}{4} = \frac{6000 \frac{\text{m}^3}{\text{day}}}{34 \frac{\text{m}^3}{\text{m}^2 \cdot \text{day}}} ; d = 15\text{m}$$

$$H = \frac{V}{S}$$

$$V = t_{RH} \cdot Q = 1.5 \text{ h} \cdot 6000 \frac{\text{m}^3}{\text{day}} \cdot \frac{1 \text{ day}}{24 \text{ h}} = 375 \text{ m}^3$$

$$H = 2.152 \text{ m}$$

b) Sludge production

Volume solids:

$$6000 \frac{\text{m}^3}{\text{day}} \cdot \frac{10^3 \text{L}}{1 \text{ m}^3} \cdot \frac{200 \text{ mg SS}}{1 \text{ L}} \cdot \frac{1 \text{ kg}}{10^6 \text{mg}} \cdot \frac{60 \text{ kg SS removed}}{100 \text{ kg SS}} = 720 \frac{\text{kg SS}_{\text{removed}}}{\text{day}}$$

$$720 \frac{\text{kg SS}_{\text{removed}}}{\text{day}} \rightarrow 0.41 \frac{\text{m}^3 \text{VS}}{\text{day}}$$

$$720 \frac{\text{kg SS}_{\text{removed}}}{\text{day}} \rightarrow 0.12 \frac{\text{m}^3 \text{FS}}{\text{day}}$$

Volume water:

$$720 \frac{\text{kg SS}_{\text{removed}}}{\text{day}} \cdot \frac{98 \text{ kg water}}{2 \text{ kg SS}_{\text{removed}}} \cdot \frac{1 \text{ m}^3}{1000 \text{ kg water}} = 35.28 \frac{\text{m}^3 \text{water}}{\text{day}}$$

Total sludge:

$$35.81 \frac{\text{m}^3 \text{sludge}}{\text{day}}$$



### Problem 7.-

a) % efficiency BOD reduction

$$\text{BOD}_1 = 60 \text{ mg} \frac{\text{O}_2}{\text{L}} = L (1 - e^{-0.23 \text{ days}^{-1} \cdot 1 \text{ days}}); L = 292.019 \text{ mg} \frac{\text{O}_2}{\text{L}}$$

$$\text{BOD}_2 = 107.7 \text{ mg} \frac{\text{O}_2}{\text{L}} = L (1 - e^{-0.23 \text{ days}^{-1} \cdot 2 \text{ days}}); L = 292.094 \text{ mg} \frac{\text{O}_2}{\text{L}}$$

$$L = L_{\text{avg}} = \frac{(292.019 + 292.094)}{2} = 292.057 \frac{\text{mg O}_2}{\text{L}}$$

$$\text{BOD}_5 = 292.057 \text{ mg} \frac{\text{O}_2}{\text{L}} (1 - e^{-0.23 \text{ days}^{-1} \cdot 5 \text{ days}}); L = 199.581 \text{ mg} \frac{\text{O}_2}{\text{L}}$$

$$\% \text{ BOD reduction} = \frac{(199.581 - 4)}{199.581} \cdot 100 = 98 \%$$

b) Surface loading factor or overflow rate and retention time

$$F_c = \frac{Q}{S} = \frac{100000 \text{ m}^3 \cdot \text{day}^{-1}}{1963.5 \text{ m}^2} = 50.93 \frac{\text{m}^3}{\text{m}^2 \cdot \text{day}}$$

$$t_{\text{RH}} = \frac{V}{Q} = \frac{1963.5 \text{ m}^2 \cdot 5 \text{ m}}{100000 \text{ m}^3 \cdot \text{day}^{-1}} \cdot \frac{24 \text{ h}}{1 \text{ day}} = 2.356 \text{ h}$$

c) Sludge production

$$320 \frac{\text{mg SS}}{\text{L}} \cdot \frac{80 \text{ mg SS}_{\text{removed}}}{100 \text{ mg SS}} = \frac{256 \text{ mg SS}_{\text{removed}}}{\text{L}}$$

$$\frac{256 \text{ mg solids}}{\text{L}} \cdot 1 \cdot 10^8 \frac{\text{L}}{\text{day}} \cdot \frac{1 \text{ kg}}{10^6 \text{ mg}} \cdot \frac{1 \text{ m}^3}{1200 \text{ kg solids}} \cdot \frac{100 \text{ m}^3 \text{ sludge}}{4 \text{ m}^3 \text{ solids}} = 533.33 \frac{\text{m}^3 \text{ sludge}}{\text{day}}$$



### Problem 8.-

a) Sludge production

$$300 \frac{\text{mg SS}}{\text{L}} \cdot \frac{70 \text{ mg SS}_{\text{removed}}}{100 \text{ mg SS}} \cdot \frac{11250 \cdot 10^3 \frac{\text{L}}{\text{day}}}{\frac{10^6 \text{kg}}{\text{mg}}} = \frac{2362.5 \text{ kg SS}_{\text{removed}}}{\text{day}}$$

$$\text{FS} = \frac{2362.5 \text{ kg SS}}{\text{day}} \cdot \frac{30 \text{ kg FS}}{100 \text{ kg SS}} = 708.75 \frac{\text{kg FS}}{\text{day}}$$

$$\text{VS (not transformed)} = \frac{2362.5 \text{ kg SS}}{\text{day}} \cdot \frac{70 \text{ kg VS}}{100 \text{ kg SS}} \cdot \frac{40 \text{ kg VS n. tr.}}{100 \text{ kg VS}} = 661.5 \frac{\text{kg VS n. tr.}}{\text{day}}$$

$$\begin{aligned} \text{Total sludge} &= \frac{(708.75 + 661.5) \text{ kg solids}}{\text{day}} \cdot \frac{100 \text{ kg sludge}}{5 \text{ kg solids}} \cdot \frac{1 \text{ m}^3 \text{ sludge}}{1000 \text{ kg sludge}} \\ &= \frac{27405 \text{ m}^3 \text{ sludge}}{\text{day}} \end{aligned}$$

b) Biogas production

$$\frac{2362.5 \text{ kg SS}}{\text{day}} \cdot \frac{70 \text{ kg VS}}{100 \text{ kg SS}} \cdot \frac{600 \text{ kg VS tr.}}{100 \text{ kg VS}} \cdot \frac{0.35 \text{ m}^3 \text{CH}_4}{1 \text{ kg VS tr.}} \cdot \frac{100 \text{ m}^3 \text{ biogas}}{50 \text{ m}^3 \text{CH}_4} = 694.58 \text{ m}^3 \text{ biogas}$$

c) Volume of anaerobic digester

$$\frac{2362.5 \text{ kg SS}}{\text{day}} \cdot \frac{100 \text{ kg sludge}}{2 \text{ kg SS}} \cdot \frac{1 \text{ m}^3 \text{ sludge}}{1000 \text{ kg sludge}} = 118.125 \frac{\text{m}^3 \text{ sludge}}{\text{day}}$$

$$V = t_R \cdot Q = 25 \text{ day} \cdot 118.125 \frac{\text{m}^3 \text{ sludge}}{\text{day}} = 2953.13 \text{ m}^3$$