

Concepto derivada

$$f'(a) = \lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a} = \lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x}$$

Tabla de derivación

$$y = k \quad \forall k \in \mathbb{R} \quad y' = 0$$

$$y = u \quad u = x \quad y' = 1$$

$$y = u \quad u = u(x) \quad y' = u'$$

$$y = k \cdot u \quad y' = k \cdot u'$$

$$y = u + v - w \quad y' = u' + v' - w'$$

$$y = u \cdot v \quad y' = u' \cdot v + u \cdot v'$$

$$y = \frac{u}{v} \quad y' = \frac{u' \cdot v - u \cdot v'}{v^2}$$

$$y = u^n \quad y' = n \cdot u^{n-1} \cdot u'$$

$$y = \sqrt[n]{u} \quad y' = \frac{u'}{n \cdot \sqrt[n]{u^{n-1}}}$$

$$y = \log_a u \quad y' = \frac{u'}{u} \log_a e$$

$$y = L(u) \quad y' = \frac{u'}{u}$$

$$y = a^u \quad y' = u' \cdot a^u \cdot L(a)$$

$$y = e^u \quad y' = u' \cdot e^u$$

$$y = u^v \quad y' = v' \cdot u^v \cdot L(u) + v \cdot u^{v-1} \cdot u'$$

$$y = \operatorname{sen} u \quad y' = u' \cdot \cos u$$

$$y = \operatorname{cos} u \quad y' = -u' \cdot \operatorname{sen} u$$

$$y = \operatorname{tg} u \quad y' = \frac{u'}{\cos^2 u} = u' (1 + \operatorname{tg}^2 u) = u' \cdot \sec^2 u$$

$$y = \operatorname{cot} u \quad y' = \frac{-u'}{\operatorname{sen}^2 u} = -u' (1 + \operatorname{cot}^2 u) = -u' \cdot \operatorname{csc}^2 u$$

$$y = \operatorname{arcsen} u \quad y' = \frac{u'}{\sqrt{1-u^2}}$$

$$y = \operatorname{arccos} u \quad y' = \frac{-u'}{\sqrt{1-u^2}}$$

$$y = \operatorname{arctg} u \quad y' = \frac{u'}{1+u^2}$$

Aplicaciones de la derivada

$$f'(a) \geq 0 \quad f(x) \text{ creciente en } x = a$$

$$f'(a) > 0 \quad f(x) \text{ estrictamente creciente en } x = a$$

$$f'(a) \leq 0 \quad f(x) \text{ decreciente en } x = a$$

$$f'(a) < 0 \quad f(x) \text{ estrictamente decreciente en } x = a$$

$$f'(a) = 0 \quad \begin{cases} f''(a) > 0 & \text{Mínimo relativo en } x = a \text{ (convexa)} \\ f''(a) < 0 & \text{Máximo relativo en } x = a \text{ (concava)} \end{cases}$$

$$f''(a) = 0 \rightarrow f'''(a) \neq 0 \rightarrow \text{Punto de inflexión en } x = a$$